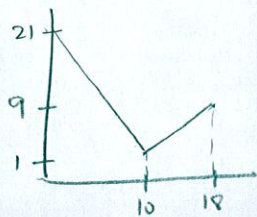


A person's velocity (in meters per minute) at time t (in minutes) is given by $v(t) = \begin{cases} 21-2t, & 0 \leq t \leq 10 \\ t-9, & 10 \leq t \leq 18 \end{cases}$. SCORE: ____ / 5 PTS

[a] Find the exact distance the person travelled from time $t = 0$ seconds to $t = 18$ seconds.

NOTE: You must show the arithmetic expression that you used to get your answer.



$$\frac{1}{2}(21+9)(10-0) + \frac{1}{2}(9+9)(18-10)$$

$$\textcircled{1} \frac{1}{2}(21+9)(10) + \frac{1}{2}(9+9)(8) \textcircled{1}$$

$$= 110 + 40$$

$$= \underline{150 \text{ m}} \textcircled{\frac{1}{2}}$$

[b] Estimate the distance the person travelled from time $t = 0$ seconds to $t = 18$ seconds using three subintervals and left endpoints.

NOTE: You must show the arithmetic expression that you used to get your answer.

$$\Delta t = \frac{18-0}{3} = 6$$

$$v(0)\Delta t + v(6)\Delta t + v(12)\Delta t$$

$$= \underline{(21+9+3)(6)} \textcircled{2}$$

$$= \underline{198 \text{ m}} \textcircled{\frac{1}{2}}$$

The graph of function f is shown on the right.

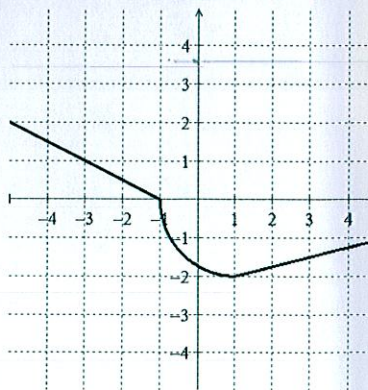
The graph consists of a diagonal line, an arc of a circle, then another diagonal line.

SCORE: _____ / 4 PTS

[a] Evaluate $\int_{-5}^5 f(x) dx$.

NOTE: You must show the arithmetic expression that you used to get your answer.

$$\begin{aligned} & \textcircled{\frac{1}{2}} \underbrace{\frac{1}{2}(4)(2)} - \underbrace{\frac{1}{4}\pi(2)^2}_{\textcircled{1}} - \underbrace{\frac{1}{2}(2+1)(4)}_{\textcircled{1}} \\ & = \underbrace{-2 - \pi}_{\textcircled{\frac{1}{2}}} \end{aligned}$$



[b] Evaluate $\int_1^{-5} f(x) dx$.

$$= - \int_{-5}^1 f(x) dx = - \left[\frac{1}{2}(4)(2) - \frac{1}{4}\pi(2)^2 \right] = \underbrace{\pi - 4}_{\textcircled{1}}$$

NO POINTS
FOR $4 - \pi$

Using the limit definition of the definite integral, and right endpoints, find $\int_{-1}^3 (3x^2 - x - 4) dx$.

SCORE: ____ / 10 PTS

NOTE: Solutions using any other method will earn 0 points.

$$\Delta x = \frac{3 - (-1)}{n} = \frac{4}{n}$$

$$\textcircled{1} \lim_{n \rightarrow \infty} \sum_{i=1}^n f\left(-1 + \frac{4i}{n}\right) \frac{4}{n}$$

$$= \lim_{n \rightarrow \infty} \left[\frac{4}{n} \sum_{i=1}^n \left[3\left(-1 + \frac{4i}{n}\right)^2 - \left(-1 + \frac{4i}{n}\right) - 4 \right] \right] \textcircled{2}$$

$$= \lim_{n \rightarrow \infty} \frac{4}{n} \sum_{i=1}^n \left(\frac{-24i}{n} + \frac{48i^2}{n^2} - \frac{4i}{n} \right)$$

$$= \lim_{n \rightarrow \infty} \frac{4}{n} \sum_{i=1}^n \left(\frac{-28i}{n} + \frac{48i^2}{n^2} \right) \textcircled{2}$$

$$= \lim_{n \rightarrow \infty} \frac{4}{n} \left(-\frac{28}{n} \sum_{i=1}^n i + \frac{48}{n^2} \sum_{i=1}^n i^2 \right)$$

$$= \lim_{n \rightarrow \infty} \frac{4}{n} \left(-\frac{28}{n} \frac{n(n+1)}{2} + \frac{48}{n^2} \frac{n(n+1)(2n+1)}{6} \right)$$

$$= 4(-14 + 16)$$

$$= 8 \textcircled{1}$$

① FOR HAVING $\lim_{n \rightarrow \infty}$

ON EACH LINE

THAT STILL INVOLVES "n"

Evaluate $\int_{-6}^6 (|x-4| - 2\sqrt{36-x^2}) dx$ using the properties of definite integrals and interpreting in terms of area. SCORE: ____ / 5 PTS

NOTE: You must show the proper use of the properties of the definite integral, NOT just the arithmetic.

$$\begin{aligned} &= \int_{-6}^6 |x-4| dx - 2 \int_{-6}^6 \sqrt{36-x^2} dx \quad \textcircled{1} = \frac{1}{2}(10)(10) + \frac{1}{2}(2 \times 2) - 2\left(\frac{1}{2}\pi(6)^2\right) \quad \textcircled{1} \\ &= 52 - 36\pi \quad \textcircled{1} \end{aligned}$$

